

Synchrone machine

S	4	Power in [KVA]
U	398.37168574084	Grid voltage Line-Line RMS
Us	230	Grid voltage Line-Neutral RMS
T	20	Load torque

Calculate

Xd	39.675[ohm]
Lm	126.289[mH]
Pmech	3141.593[Watt]
v	0.903[Rad]
lasthoek	51.758[Degrees]
Ie	8.198[A]
Epx	-255.466[V]
Epy	201.339[V]
Exx	255.466[V]
Exy	123.931[V]
I _{sx}	3.124[A]
I _{sy}	-6.439[A]
I _s ^{rms}	5.061[A]
cos(phi)	0.900[.]
Pcalculated	3141.593[Watt]

Synchronous Machine

$$S[\text{VA}] = 4000[\text{kVA}]$$

$$S_b[\text{VA}] = S/3 = 1333[\text{kVA}] \text{ per phase}$$

Line and neutral voltage:

$$U[\text{V}] = 230[\text{Vrms Line-Neutral}] * \sqrt{3} = 398[\text{Vrms Line-Line}]$$

Mechanical power:

$$T_e = 20[\text{Nm}] \text{ and } n = 3000/2 \Rightarrow \omega = 157.1[\text{Rad/s}]$$

$$P[\text{Watt}] = T_e * \omega = 20 * 157 = 3142[\text{Watt}]$$

Calculate base impedance:

$$Z_b[V] = U^2/S_b = 230*230/1333 = 52900/1333 = 39.68$$

Assume 1pu for the synchronous impedance/inductance:

$$X_d[\text{ohm}] = Z_b * 1\text{p.u.} = 40[\text{ohm}]$$

$$L_d[\text{mH}] = X_d/314.15927 = 39.68/314.15927 = 126[\text{mH}]$$

Calculate load angle from power equation:

$$\sin(\nu) = P_m/S = 3142/4000 = 0.785$$

$$\nu = \arcsin(0.785) = 0.9[\text{Rad}] = 52[\text{degrees}]$$

Calculate I_e in case of nominal operation, so $E_p = U_s$

$$I_e = U * \sqrt{2} / X_d = 1.414 * 230 / 39.68 = 325 / 39.68 = 8.2[\text{A}]$$

Calculate the induced back emf from the rotorfield:

$$E_{px}[\text{v}] = -\sqrt{2} * U * \sin(\nu) = -\sqrt{2} * 230 * \sin(0.9) = -255[\text{v}]$$

$$E_{py}[\text{v}] = \sqrt{2} * U * \cos(\nu) = \sqrt{2} * 230 * \cos(0.9) = 201[\text{v}]$$

Note that we are using the maximum amplitude of the voltage, while calculating voltages and currents!

Calculate the voltage U_x between the induced back emf and the grid voltage:

$$U_x(x)[\text{v}] = 0 - E_{px} = 0 - (-255) = 255[\text{v}]$$

$$U_x(y)[\text{v}] = \sqrt{2} * U_s - E_{py} = 325 - 201 = 124[\text{v}]$$

$$I = U_x / X_d$$

Stator current lags U_x with 90 degrees:

with xy components $I_x = U_x(y) / X_d$ and $I_y = -U_x(x) / X_d$

$$I_x = U_x(y) / X_d = 124 / 39.68 = 3.1$$

$$I_y = -U_x(x) / X_d = -255 / 39.68 = -6.4$$

RMS value of the stator current:

$$I_s = \sqrt{I_x^2 + I_y^2} / \sqrt{2} = \sqrt{10 + 41} / 1.414 = 5.06$$

and the $\cos(\phi)$

$$\cos(\phi) = -\cos(\text{atan2}(I_x, I_y)) = -\cos(\text{atan2}(3.1, -6.4)) = 0.9$$

from which we can recalculate and check the real power:

$$P = 3 * U_s * I_s * \cos(\phi) = 230 * 5.06 * 0.9 = 3142$$

$$S = 3 * U_s * I_s * \cos(\phi) = 230 * 5.06 * 0.9 = 3492$$