

# Cos( $\phi$ ) compensation

P	7000	Load Power [Watt]
U	230	Load rms Line-Neutral voltage
cos( $\phi$ )	0.85	Load cos( $\phi$ )
R <sub>cable/meter</sub>	0.01	Cable resistance per meter[ $\Omega$ per meter]
L <sub>cable/meter</sub>	1.0E-5	Cable inductance per meter[H per meter]
Cable length	25	Cable length [meter]

Calculate

## Calculate nominal power

Load parameters P and cos( $\phi$ ) are defined for U without cable

$$\text{Apparent power per phase } S[\text{VA}] = P/\cos(\phi) = 8235[\text{VA}]$$

$$Q[\text{VAR}] = \sqrt{S^2 - P^2} = \sqrt{8235^2 - 7000^2} = 4338[\text{VAR}]$$

$$I_{\text{nom}}[\text{A}] = S/U = 8235/230 = 35.806[\text{A}]$$

## Calculate load resistance

From P and I the load resistance is calculated:

$$R_{\text{load}}[\text{ohm}] = P/I^2 = 7000/(35.806^2) = 5[\text{ohm}]$$

## Calculate load inductance

From reactive power, the load inductance is calculated

$$X_{\text{load}} = Q/I^2 = 4338/(35.806^2) = 3.384[\text{ohm}]$$

$$L_{\text{load}}[\text{mH}] = X_{\text{load}}/(2 \pi f) = 3/314.15927 = 10.8[\text{mH}]$$

## Calculate cable resistance and inductance

$$R_{\text{cable}}[\text{m}\Omega] = R_{\text{cable}}[\text{per meter}] * \text{length} [\text{per phase}] = 10 * 25 = 250[\text{m}\Omega]$$

$$L_{\text{cable}}[\text{mH}] = L_{\text{cable}}[\text{per meter}] * \text{length} [\text{per phase}] = 0.01 * 25 = 0.25[\text{mH}]$$

$$X_{\text{cable}}[\Omega] = L_{\text{cable}} * 2 \pi f = 0.25 * 314.15927 = 0.079[\Omega]$$

$$Z_{\text{cable}}[\Omega] = \sqrt{R_{\text{cable}}^2 + X_{\text{cable}}^2} = \sqrt{0.25^2 + 0.079^2} = 0.262[\Omega]$$

## Calculate total resistance and inductance seen from the source

$$R_{\text{tot}}[\Omega] = R_{\text{cable}} + R_{\text{load}} = 0.25 + 5 = 5.71[\Omega]$$

$$L_{\text{tot}}[\text{mH}] = L_{\text{cable}} + L_{\text{load}} = 0.25 + 0 = 11.021[\text{mH}]$$

$$X_{\text{tot}}[\Omega] = L_{\text{tot}} * 2 \pi f = 11.021 * 314.15927 = 3.462[\Omega]$$

$$Z_{\text{tot}}[\Omega] = \sqrt{R_{\text{tot}}^2 + X_{\text{tot}}^2} = \sqrt{5.71^2 + 3.462^2} = 6.678[\Omega]$$

### **Calculate new current**

$$I_{\text{new}} = U / Z_{\text{tot}} = 230 / 6.678 = 34.44[\text{A}]$$

### **Calculate apparent power**

$$S = U * I_{\text{new}} = 230 * 34.443 = 7922[\text{VA}]$$

### **Calculate Cable loss**

$$R_{\text{cable}} * I_{\text{new}}^2 = 0 * 34.443^2 = 297[\text{Watt}]$$

### **Calculate power delivered to the load**

$$R_{\text{load}} * I_{\text{new}}^2 = 5 * 34.443^2 = 6477[\text{Watt}]$$

### **Calculate Load voltage**

$$U_{\text{load new}} = U - Z_{\text{cable}} * I_{\text{new}} = 230 - 0 * 34.443 = 221[\text{Volt}]$$

### **Calculate new cos( $\phi$ )**

$$\text{Cos}(\phi) = (P_{\text{cable}} + P_{\text{load}}) / S = (297 + 6477) / 7922 = 0.855$$

### **Calculate Reactive power for calculating the compensation capacitor**

$$Q[\text{VAR}] = \sqrt{S^2 - (P_{\text{cable}} + P_{\text{load}})^2} = \sqrt{7922^2 - 6773.81^2} = 4107[\text{VAR}]$$

### **Calculate compensation capacitor**

$$X_c = U^2 / Q = 230^2 / 4107 = 13[\Omega]$$

$$C = 1 / (2\pi * f * X_c) = 1 / (314.15927 * 13) = 247[\mu\text{F}]$$